



$C(? , k)$

$M(1, 6)$   $r=?$

$N(5, -2)$

$P(0, k)$

$$(1) \quad (x-h)^2 + (y-k)^2 = r^2$$

$\uparrow$   $x_c$                        $\uparrow$   $y_c$

$$\boxed{(1-h)^2 + (6-k)^2 = r^2}$$

$$(2) \quad (5-h)^2 + (-2-k)^2 = r^2$$

$$\boxed{(5-h)^2 + (2+k)^2 = r^2}$$

$$(3) \quad (0-h)^2 + (k-k)^2 = r^2$$

$$\boxed{h^2 = r^2}$$

$\hookrightarrow h = \pm r$   
 $h > 0, \boxed{h=r}$

$$\begin{cases} (1-r)^2 + (6-k)^2 = r^2 \\ (5-r)^2 + (2+k)^2 = r^2 \end{cases}$$

$$1 - 2r + r^2 + 36 - 12k + k^2 = r^2$$

$$25 - 10r + r^2 + 4 + 4k + k^2 = r^2$$

$$\rightarrow \begin{cases} 37 - 2r - 12k + k^2 = 0 \\ 29 - 10r + 4k + k^2 = 0 \end{cases} \text{ we subtract the two.}$$

$$8 + 8r - 16k = 0 \rightarrow 1 + r - 2k = 0$$

$$\boxed{r = 2k - 1}$$

$$k^2 - 12k + 37 - 2(2k - 1) = 0$$

$$k^2 - 12k + 37 - 4k + 2 = 0$$

$$k^2 - 16k + 39 = 0$$

$$(k - 13)(k - 3) = 0$$

$$(k - 13) = 0 \text{ or } k - 3 = 0$$

$$k = 13 \text{ or } k = 3$$

$$\begin{cases} \rightarrow r = 2(13) - 1 \\ r = 25 \\ h = 25 \end{cases}$$

$$r = 2(3) - 1$$

$$r = 6 - 1$$

$$r = 5, h = 5$$

$$\hookrightarrow \boxed{(x - 5)^2 + (y - 3)^2 = 25}$$

$$\hookrightarrow \boxed{(x - 25)^2 + (y - 13)^2 = 625}$$