

Sketch the graph of

$$y = 2x^3 + 7x^2 + 2x - 3$$

$$-3: \pm 1, \pm 3$$

$$2: \pm 1, \pm 2$$

Testing values: $\pm 1, \pm \frac{1}{2}, \pm 3, \pm \frac{3}{2}$

$$f(-1) = 0 \rightarrow (x+1) \text{ is a factor}$$

$$f\left(\frac{1}{2}\right) = 0 \rightarrow (2x-1) \text{ is a factor}$$

$$f(-3) = 0 \rightarrow (x+3) \text{ is a factor}$$

$$\therefore f(x) = (2x-1)(x+1)(x+3)$$

$$\text{The leading coefficient: } (2)(1)(1) = 2$$

$$\text{The constant term: } (-1)(1)(+3) = -3$$

(Full) factored form:

$$y = 2\left(x - \frac{1}{2}\right)(x+1)(x+3)$$

$$\text{degree} = 3 \leftarrow \text{odd}, \text{ lead coeff} = 2 > 0$$

$\mathbb{Q} \text{ III to } \mathbb{Q} \text{ I}$

