

## Thinking Questions

6) Determine if  $f(x) = (x-3)(x+4)(2x-8)(3+x)$  is odd, even or neither.

Solution

Rewrite

$$f(x) = 2(x-3)(x+4)(x-4)(x+3)$$

$$f(x) = 2(x^2-9)(x^2-16)$$

$$f(x) = 2[x^4 - 16x^2 - 9x^2 + 144]$$

$$f(x) = 2x^4 - 32x^2 - 18x^2 + 288$$

$$f(x) = 2x^4 - 50x^2 + 288$$

$$f(-x) = 2(-x)^4 - 50(-x)^2 + 288$$

$$f(-x) = 2x^4 - 50x^2 + 288 = f(x)$$

$\therefore f(x)$  is even.