

Find a unit vector that is parallel to the xy -plane and perpendicular to the vector $4\hat{i} - 3\hat{j} + \hat{k}$

$$4\hat{i} - 3\hat{j} + \hat{k} = (4, -3, 1)$$

$$\text{let } \vec{u} = (u_1, u_2, u_3)$$

$$\text{If } \vec{a} \perp \vec{b}, \vec{a} \cdot \vec{b} = 0$$

$$(4, -3, 1) \cdot (u_1, u_2, u_3) = 0$$

$$4u_1 - 3u_2 + u_3 = 0$$

$$(u_1, u_2, u_3) \cdot (0, 0, 1) = 0$$

Parallel to xy -plane means \perp to \hat{k}

$$u_3 = 0$$

$$u_3 = 0 \checkmark \quad \text{Substitute into } 4u_1 - 3u_2 + u_3 = 0$$

$$4u_1 - 3u_2 = 0$$

$$u_1 = \frac{3}{4}u_2, \text{ and our vector becomes}$$

$$\left(\frac{3}{4}u_2, u_2, 0\right) =$$

or, a simpler version $\rightarrow u_2 \left(\frac{3}{4}, 1, 0\right)$

Unit vector means a magnitude of 1.

$$\frac{9}{16}u_2^2 + u_2^2 = 1$$

$$\frac{25}{16}u_2^2 = 1$$

$$u_2^2 = \frac{16}{25}, \quad u_2 = \pm \sqrt{\frac{16}{25}}$$

$$u_2 = \frac{4}{5} \quad \text{or} \quad u_2 = -\frac{4}{5}$$