

$$\text{lcm}(a, b) \cdot \text{gcd}(a, b) = a \cdot b.$$

$$a = p_1^{e_1} \cdot p_2^{e_2} \cdot \dots \cdot p_k^{e_k}$$

$$b = p_1^{a_1} \cdot p_2^{a_2} \cdot \dots \cdot p_k^{a_k}$$

$$\text{lcm}(a, b) = p_1^{\max(a_1, e_1)} \cdot p_2^{\max(a_2, e_2)} \cdot \dots \cdot p_k^{\max(a_k, e_k)}$$

$$\text{gcd}(a, b) = p_1^{\min(a_1, e_1)} \cdot p_2^{\min(a_2, e_2)} \cdot \dots \cdot p_k^{\min(a_k, e_k)}$$

$$\text{lcm}(a, b) \cdot \text{gcd}(a, b)$$

$$= p_1^{\max(a_1, e_1) + \min(a_1, e_1)} \cdot p_2^{\max(a_2, e_2) + \min(a_2, e_2)} \cdot \dots \cdot p_k^{\max(a_k, e_k) + \min(a_k, e_k)}$$

∴ Aside:

$$\max(x, y) + \min(x, y) = x + y$$

$$= p_1^{a_1 + e_1} \cdot p_2^{a_2 + e_2} \cdot p_3^{a_3 + e_3} \cdot \dots \cdot p_k^{a_k + e_k}$$

$$= \underbrace{(p_1^{e_1} \cdot p_2^{e_2} \cdot \dots \cdot p_k^{e_k})}_a \cdot \underbrace{(p_1^{a_1} \cdot p_2^{a_2} \cdot \dots \cdot p_k^{a_k})}_b = ab.$$

$$\begin{array}{r} \textcircled{1} \quad 184 \mid 2 \\ \quad 92 \mid 2 \\ \quad \quad 46 \mid 2 \\ \quad \quad \quad 23 \mid 23 \\ \quad \quad \quad \quad \textcircled{1} \end{array}$$

$$184 = 2^3 \cdot 23 \checkmark$$

$$\begin{array}{r} 138 \mid 2 \\ \quad 69 \mid 3 \\ \quad \quad 23 \mid 23 \\ \quad \quad \quad \textcircled{1} \end{array}$$

$$138 = 2 \cdot 3 \cdot 23 \checkmark$$

$$\text{gcd}(184, 138) = 2 \cdot 23 = 46 \text{ packages.}$$

$$\frac{184}{46} = 4 \text{ oranges per package.}$$

$$\frac{138}{46} = 3 \text{ chocolates per package.}$$